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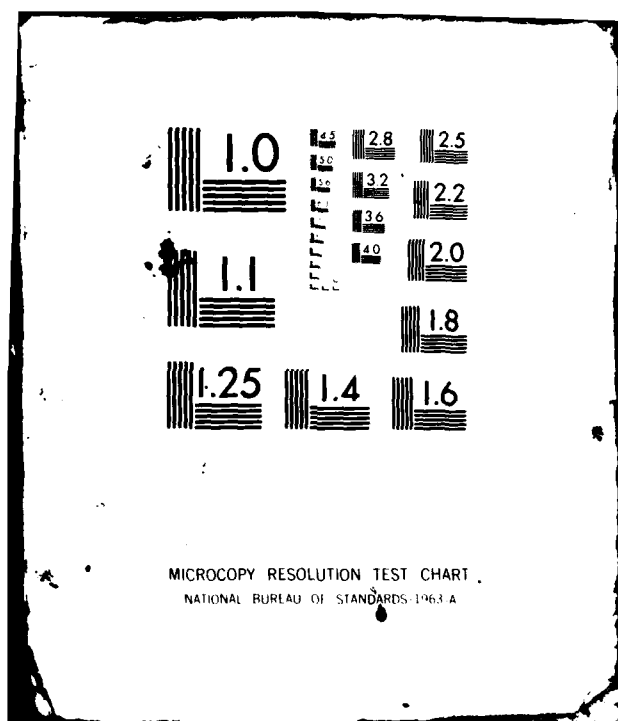
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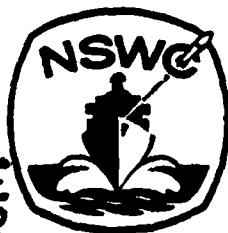
**COMMENTS ON THE DOUBLY ASYMPTOTIC
APPROXIMATION: I. KINETIC ENERGY AT
PRESSURE CUTOFF**

BY DAVID W. NICHOLSON AND MARTIN H. MARCUS
RESEARCH AND TECHNOLOGY DEPARTMENT

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report uses the Doubly Asymptotic Approximation to consider the shock wave energy available for damage in structures attacked by underwater warheads. In particular, we estimate the cutoff kinetic energy for an infinite unrestrained air-backed flat plate on which an exponentially decaying acoustic wave is incident. A comparison is given for the titanium and steel at equal plate thickness. Similarly, a comparison is given for conventional warheads and copper-lined shaped charge warheads with equal peak pressures. Over such a range of conditions there is a greatly varying ratio of pressure decay times to		

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structural response times. As expected, there is also considerable variation in the energy developed in the plate.

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FOREWORD

The ultimate objective of ^{this} the work presented here is the direct prediction of the onset and details of submarine pressure hull rupture caused by underwater explosive attack. The immediate objective of this work is to bring out some of the implications of an important analytical tool known as the Doubly Asymptotic Approximation. The results reported here provide an indication of the effect of using light structural materials such as titanium and of using nonconventional warheads such as copper-lined shaped charge warheads. *See page 3A*

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INTRODUCTION

The ultimate objective of the present work is the prediction of submarine structural response to underwater explosions. A major element in the physics is fluid-structure interaction by virtue of which pressures exerted by the fluid are relieved as the structure complies. Even though fluid-structure interaction comprises a formidable modeling problem, there has been some success treating it using a simplification known as the Doubly Asymptotic Approximation (DAA) [1]. Here we illustrate some consequences of the DAA in a model problem involving an exponentially decaying acoustic wave impinging on an infinite air-backed unrestrained flat plate, as illustrated in Figure 1.

DOUBLY ASYMPTOTIC APPROXIMATION

For the model problem the incident pressure is subject to exponential decay typical of underwater explosions:

$$p_I = p_0 \exp(-t/\theta)$$

The total pressure on the plate may be thought of as the sum of the incident pressure, the reflected pressure, and the radiated pressure arising from plate compliance:

$$p_T = p_I + p_R + p_r$$

The DAA uses the approximations

$$p_R = p_I \quad p_r = -\rho c v$$

where ρ is the water density, c is the acoustic wave speed, and v is the plate velocity. ¹⁻³

The equilibrium equation becomes

$$\begin{aligned} m \frac{dv}{dt} &= p_T \\ &= 2p_0 \exp(-t/\theta) - \rho c v \end{aligned}$$

¹ Geers, T. L., "Transient Response Analysis of Submerged Structures," in Finite Element Analysis of Transient Nonlinear Structural Behavior, ASME, 1975.

² Kennard, E. H., "The Effect of Pressure Wave on a Plate or Diaphragm," in Underwater Explosion Research, Office of Naval Research, 1950.

³ Taylor, G. I., "The Distortion Under Pressure of a Diaphragm which is Clamped Along its Edge and Stressed Beyond its Elastic Limit," in Underwater Explosion Research, Office of Naval Research, 1950.

where m is the plate mass per unit area. Now using the dimensionless quantities

$$w = v/c \quad \tau = t/\theta$$

$$\kappa = \rho c \theta / m \quad v = 2p_0 \theta / cm$$

the equation (1) may be rewritten

$$\frac{dw}{d\tau} + \kappa w = v \exp(-\tau). \quad (2)$$

With the initial condition $w(0) = 0$, the solution of (2) is

$$w = \frac{v}{1-\kappa} [\exp(-\kappa\tau) - \exp(-\tau)] \quad (3)$$

KINETIC ENERGY AT CUTOFF

Cutoff occurs when the total pressure due to the shock loading vanishes. We assume that no shockwave energy is transferred to the plate after cutoff. However, in reality, a considerable amount of energy may be transferred by afterflow, bubble pulses, etc. This has to be the subject of a subsequent analysis. The kinetic energy at cutoff should be considered the shock wave energy available for damage. Pressure cutoff therefore occurs when

$$\rho c v = 2p_0 \exp(-t/\theta)$$

and hence when

$$\kappa w = v \exp(-\tau). \quad (4)$$

Substituting (4) into (3) and solving for the cutoff time τ_c leads to

$$\tau_c = -\ln \kappa / (1-\kappa)$$

The cutoff velocity is w_c where

$$\begin{aligned} w_c &= \frac{v}{\kappa} \exp(-\tau_c) \\ &= v \left(\frac{1}{1-\kappa} \right) \end{aligned}$$

Most importantly, the kinetic energy at cutoff is

$$\begin{aligned} K_c &= \frac{1}{2} m v_c^2 \\ &= \mu \theta \kappa \left(\frac{1+\kappa}{1-\kappa} \right) \end{aligned} \quad (5)$$

where $\mu = 2p_0^2 / \rho c$

The prominence of the quantity $\kappa = \rho c \theta / m$ illustrates the physics very succinctly. It is nothing but the ratio of pressure decay times to structural (inertial) response times.

COMPUTATIONAL RESULTS

Computations are now presented for two cases.

Case 1: Here the time constant θ is held fixed and only the mass m is varied. This corresponds to comparisons of the effect of using titanium in place of steel.

An appropriate dimensionless counterpart of the cutoff kinetic energy is given by $x_1 = K_c/\mu\theta$, for which

$$x_1 = \kappa^{\frac{1+\kappa}{1-\kappa}}$$

The limiting cases of x_1 are

$$\lim_{\kappa \rightarrow 0} x_1 = 0$$

$$\lim_{\kappa \rightarrow \infty} x_1 = 0$$

$$\lim_{\kappa \rightarrow 1} x_1 = e^{-2} = .135$$

The maximum value of x_1 corresponds to $\kappa = 1$. It should be recalled that $\kappa = \rho c \theta / m$ and so κ is inversely proportional to m .

The dependence of kinetic energy at cutoff on plate mass, represented by the function $x_1(\kappa)$, is shown in Figure 2. Illustrative examples of these results will be given in the next section.

Case 2: Here the mass m is fixed, while only the time constant θ is allowed to vary. Now a dimensionless counterpart of the cutoff kinetic energy is $x_2 = K_c/\lambda$ where $\lambda = 2p_0^2 m / \rho^2 c^2$, for which

$$x_2 = \kappa^{2/(1-\kappa)}$$

This quantity has the limiting cases

$$\lim_{\kappa \rightarrow 0} x_2 = 0$$

$$\lim_{\kappa \rightarrow \infty} x_2 = 1$$

$$\lim_{\kappa \rightarrow 1} x_2 = e^{-2} = .135$$

Unlike x_1 , the maximum of x_2 occurs at $\kappa \rightarrow \infty$ and not at $\kappa = 1$.

The dependence of kinetic energy at cutoff on decay time θ , represented by the function $x_2(\kappa)$, is shown in Figure 3. Recall that κ is directly proportional to θ . Illustrative examples of these results will be given in the next section.

EXAMPLES

For the conventional UNDEX explosive represented by 50 pounds of TNT at 300 feet standoff, reference 2 gives the value

$$\theta_1 = 7 \cdot 10^{-4} \text{ sec.}$$

For a copper-lined shaped charge warhead fired under water, we found some data from which we estimated the decay time as

$$\theta_2 = 3.5 \cdot 10^{-5} \text{ sec.}$$

For a one inch thick steel plate

$$(m/\rho c)_1 = 1.3 \cdot 10^{-4} \text{ sec}$$

while for a one inch thick titanium plate

$$(m/\rho c)_2 = 0.78 \cdot 10^{-4} \text{ sec}$$

We may form the following table:

	<u>Conventional</u>	<u>Copper Jet</u>
	$\kappa, x_1 / .135, x_2$	$\kappa, x_1 / .135, x_2$
steel	5.38, 0.638, 0.464	0.27, 0.759, 0.028
titanium	8.97, 0.476, 0.579	0.45, 0.903, 0.055

The values of $x_1 / .135$ suggest that a titanium flat plate develops about 15-30% less cutoff kinetic energy than a steel flat plate with the same plating thicknesses. The values of x_2 suggest that, for both metals and a fixed incident pressure amplitude p_0 , the cutoff kinetic energy for a shaped charge jet is a small fraction of that for a conventional warhead.

DISCUSSION

The Doubly Asymptotic Approximation has been used to investigate the consequences of certain target and warhead variations on the shock wave energy available for damage. At similar plate thickness, a titanium structure may develop 15-30% less energy than a steel structure. At the same incident pressure amplitudes, a copper-lined shaped charge warhead may introduce only a small fraction of the energy introduced by a conventional warhead.

REFERENCES

1. Geers, T. L., "Transient Response Analysis of Submerged Structures," in Finite Element Analysis of Transient Nonlinear Structural Behavior, ASME, 1975.
2. Kennard, E. H., "The Effect of a Pressure Wave on a Plate or Diaphragm," in Underwater Explosion Research, Office of Naval Research, 1950.
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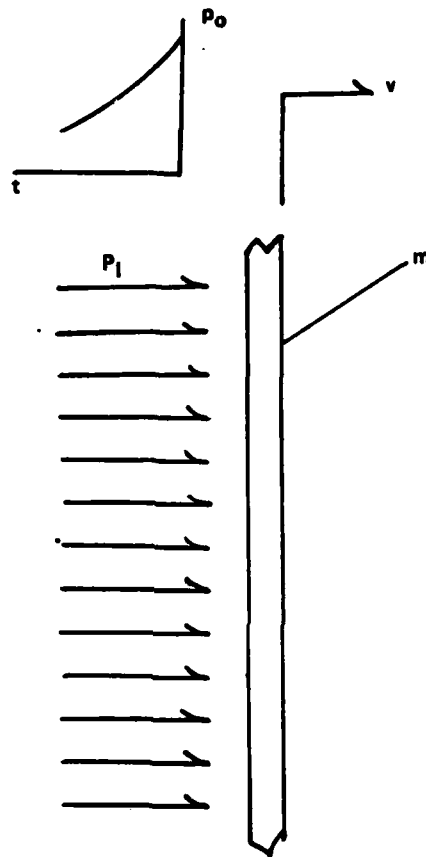


FIGURE 1 EXPONENTIALLY DECAYING PLANE WAVE INCIDENT ON
AN UNRESTRAINED AIRBACKED PLATE IN AN ACOUSTIC FLUID

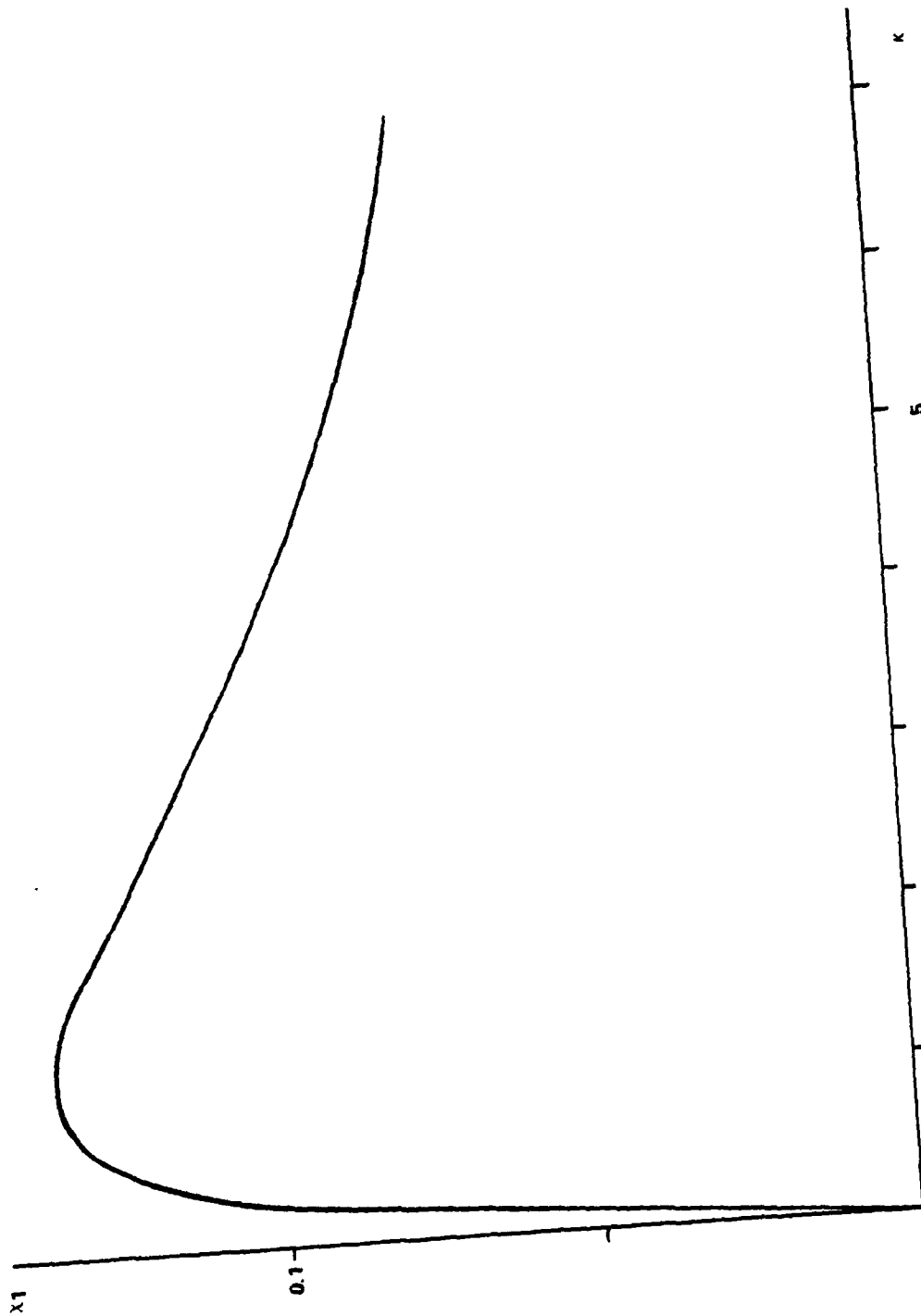


FIGURE 2 EFFECT OF PLATE MASS ON THE KINETIC ENERGY AT CUTOFF

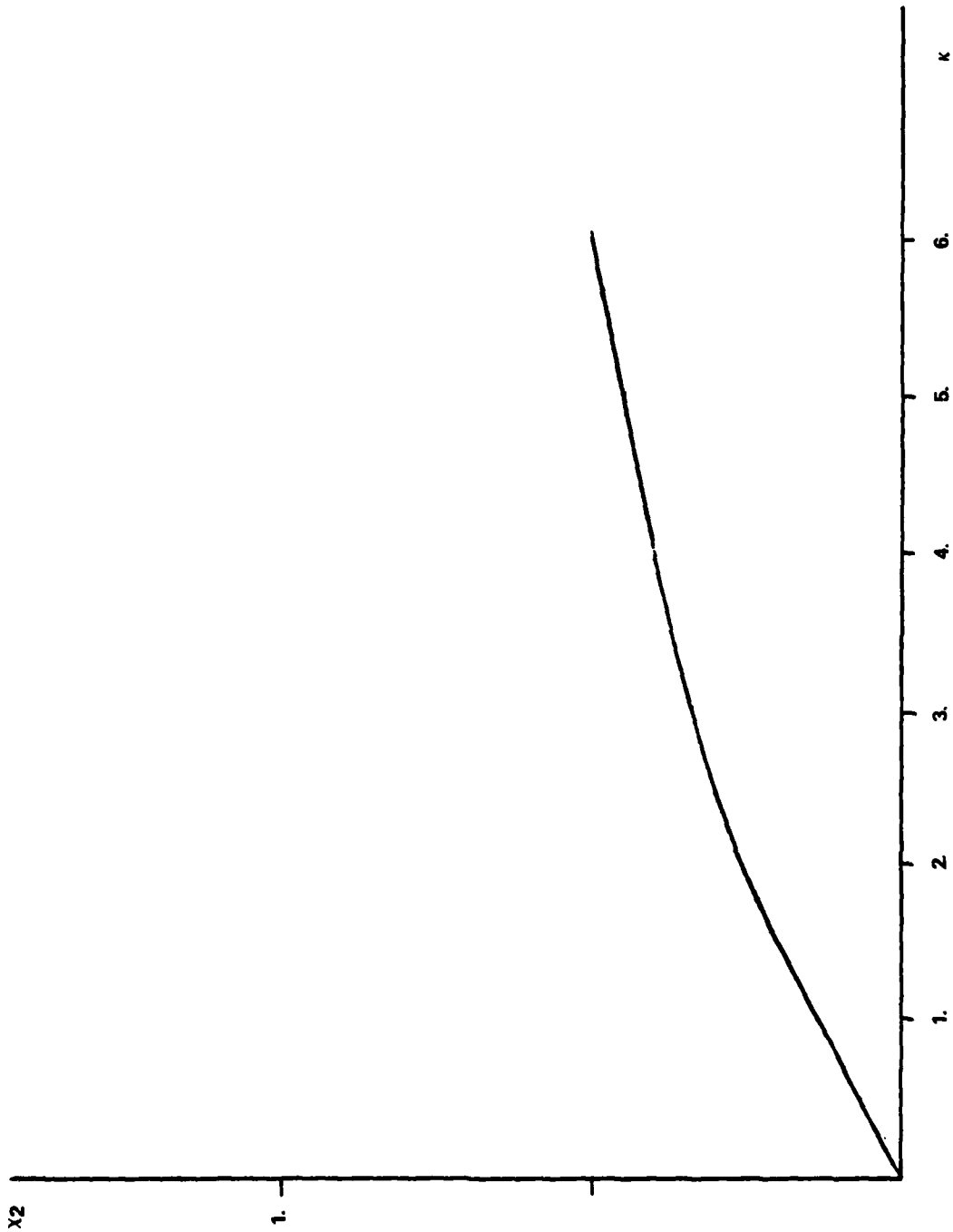


FIGURE 3 EFFECT OF TIME CONSTANT ON THE KINETIC ENERGY AT CUTOFF

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